

# *Bubbles and Debt Crises*

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# Outline

- ▶ What drives bubbles?
  - ▶ a simple framework building on short-sales constraints and heterogeneous beliefs
  - ▶ capture both asset overvaluation and trading frenzy, which are commonly observed in historical bubbles
- ▶ How are bubbles financed?
  - ▶ collateralized debt—high leverage and short maturity, joint booms in asset and credit markets
  - ▶ failure to roll over short-term debt triggers a crisis

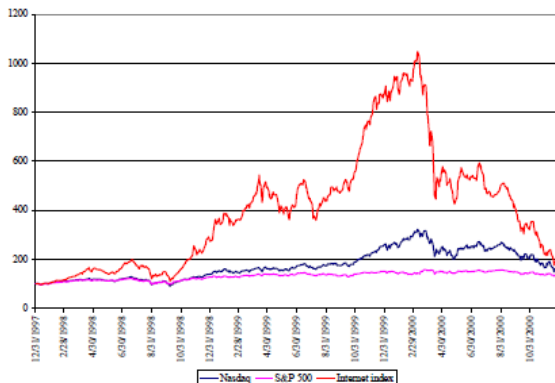
## *Part I: Bubbles*

- ▶ The crisis followed two great bubbles: the Internet bubble and the housing bubble.
  - ▶ The burst of the Internet bubble led to an expansionary US monetary policy for a prolonged period.
  - ▶ The low interest rate together with financial innovations such as securitization of subprime mortgages had fueled housing speculation and led to a great housing bubble.
  - ▶ The burst of the housing bubble eroded the balance sheets of many financial institutions, and eventually dragged down the world economy.

# What Do We Know About Bubbles?

- ▶ It is common to see price bubbles in new technologies, such as railroad, radio, biotech, Internet, securitization, . . .

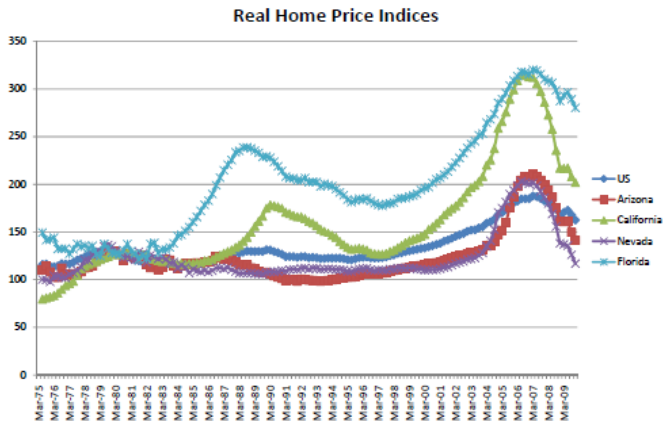
The Internet Bubble



## *Some Basic Facts about the Internet Bubble*

- ▶ Lamont and Thaler (2003, JPE)
  - ▶ Palm-3Com Case: Palm was valued at 20 billion dollars more than its parent company 3Com.
  - ▶ Shorting Palm stocks is difficult as it is difficult to borrow the shares.
- ▶ Ofek and Richardson (2003, JF)
  - ▶ In Feb 2000, the internet sector has roughly 400 companies, largely profitless.
  - ▶ The sector commanded about 6% of the market capitalization.
  - ▶ An astounding 20% of trading volume.
- ▶ Hong and Stein (2007, JEP)
  - ▶ A positive cross-sectional correlation for Nasdaq stocks between market-to-book ratio and trading volume.

# The Housing Bubble



## *Some Basic Facts about the Housing Bubble*

- ▶ The high flying areas such as California, Nevada, Arizona and Florida also had unusually high level of investment home purchases, as high as one third of the transactions.
- ▶ The housing boom was especially strong in subprime areas, e.g., Mian and Sufi (2009).

# The Chinese Warrants Bubble



## *Some Basic Facts about the Chinese Warrants Bubble*

- ▶ Xiong and Yu (2009)
  - ▶ 17 deeply out-of-the-money put warrants were traded nearly 300% each day at an average price of 0.48 Yuan.
  - ▶ Daily Yuan dollar can reach 45 billion Yuan (\$7 billion).
- ▶ Bubble can arise even when the asset fundamentals are publicly observable.
- ▶ Bubble can arise even when the asset maturity is predetermined and finite.

# *The Classic Asset Pricing Theories*

- ▶ Classic asset pricing theories stress that asset prices are determined by asset fundamentals, i.e., expected future cashflows and risk premium for bearing the risk.
- ▶ Capital Asset Pricing Model (CAPM) by Markowitz and Sharpe: risk premium is determined by market risk.
- ▶ No-arbitrage pricing theory by Black, Scholes, Merton, Ross: arbitrage trading by smart money would eliminate price deviation from fundamentals caused by irrational investors.
- ▶ Efficient market hypothesis by Fama: asset prices efficiently incorporate relevant information and leave no profit opportunities in the market.

# *A Simple Framework for Bubbles*

- ▶ Two basic ingredients:
  - ▶ Short-sales constraints
  - ▶ Heterogeneous beliefs
- ▶ Key idea: asset prices are upward biased because of the short-sales constraints; time-varying beliefs lead to resale options, which further push up the prices.
- ▶ Growing literature building on this framework:
  - ▶ Miller (1977, JF), Harrison and Kreps (1978, QJE), Morris (1996, QJE), Scheinkman and Xiong (2003, JPE), Hong, Scheinkman and Xiong (2006, JF).

## Short-Sales Constraints

- ▶ Shorting is difficult/illegal in many markets:
  - ▶ Houses cannot be sold short.
  - ▶ Shorting is illegal in China and various countries.
  - ▶ Shorting is allowed in US and other developed markets, but requires borrowing of the asset which can be difficult.
- ▶ Mutual funds, pension funds and insurance companies tend to restrict short-selling.
  - ▶ Broadly speaking, many institutions are reluctant to short-sell overvalued assets because of agency problems, e.g., He and Xiong “Multi-market Delegated Asset Management”.
  - ▶ Payoff from shorting is negatively skewed—hard to prevent risk-seeking.

# Heterogeneous Beliefs

- ▶ Heterogeneous prior beliefs
  - ▶ People tend to hold different views about new things, such as new technologies, new securities, etc.
  - ▶ Game theory models impose a common-prior assumption (Harsanyi doctrine) for convenience, rather than for economic reasons (e.g., Morris, 1995).
  - ▶ Beliefs eventually converge in the long run.
- ▶ Heterogeneous learning rules
  - ▶ Overconfidence can lead agents to overvalue their favorite signals (e.g., Scheinkman and Xiong, 2003)
  - ▶ Uncertain environment can prevent agents from agreeing on their learning models (Acemoglu, Chernozhukov, and Wold, 2009)

## A Static Model

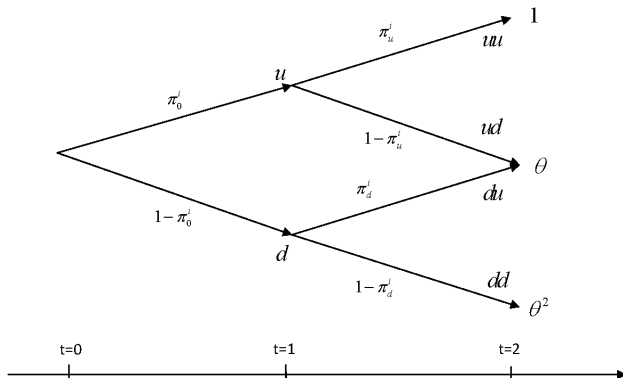
- ▶ Consider a setting with two dates:  $t = 0, 1$ . There is one risky asset with a random liquidation value of  $\tilde{\theta}$  at  $t = 1$ .
  - ▶  $\tilde{\theta}$  can be 1 or 0 with probabilities of  $\pi$  or  $1 - \pi$ .
  - ▶  $\pi$  is unknown to the public.
- ▶ Suppose that  $\pi = 0.5$ , but agents disagree about its value:
  - ▶ one group believes that its value is  $\pi^h = 0.5 + \delta$ ;
  - ▶ the other group believes that it is  $\pi^l = 0.5 - \delta$ .
- ▶ Suppose that short-sales are not allowed; agents are risk-neutral; and interest rate is zero.

## A Static Model (cont'd)

- ▶ What is the asset price at  $t = 0$ ?
  - ▶  $p_0 = 0.5 + \delta$ , which increases with  $\delta$ .
  - ▶ The key insight of Miller (1977).
- ▶ The expected return measured by an objective econometrician:
  - ▶  $E_0 \left( \tilde{\theta} \right) - p_0 = -\delta$ , which decreases with  $\delta$ .
- ▶ Empirical evidence:
  - ▶ Diether, Malloy and Scherbina (2002): stocks with higher dispersion in analysts' earnings forecasts tend to have lower returns.

# A Dynamic Model

- Consider a setting with three dates:  $t = 0, 1$  and two groups of agents,  $h$  and  $l$ .



## A Dynamic Model (cont'd)

- ▶ The objective probability of an up move is always 0.5 and  $\theta = 0.4$ .
  - ▶ The fundamental prices are
    - ▶  $f_u = 0.5 \times 1 + 0.5\theta = 0.7$ ;
    - ▶  $f_d = 0.5\theta + 0.5\theta^2 = 0.28$ ;
    - ▶  $f_0 = 0.5p_u + 0.5p_d = 0.49$ .
- ▶ Consider a basic case: for any  $n \in \{0, u, d\}$ ,  $\pi_n^h = 0.6 > \pi_n^l = 0.4$ .
  - ▶ The  $h$ -group determines the prices:
    - ▶  $p_u = 0.6 \times 1 + 0.4\theta = 0.76$ ;
    - ▶  $p_d = 0.6\theta + 0.4\theta^2 = 0.304$ ;
    - ▶  $p_0 = 0.6p_u + 0.4p_d = 0.5776$ .

## A Dynamic Model (cont'd)

- ▶ Suppose that  $\pi_0^h = 0.6$ ,  $\pi_0^l = 0.4$ ;  $\pi_u^h = 0.6$ ,  $\pi_u^l = 0.8$  ( $l$ -group becomes more optimistic in state  $u$ );  $\pi_d^h = 0.6$ ,  $\pi_d^l = 0.4$ .
  - ▶ The initially more optimistic  $h$ -group has a resale option in state  $u$ :
    - ▶  $p_u = 0.8 \times 1 + 0.2\theta = 0.88$  (by  $l$ -group);
    - ▶  $p_d = 0.6\theta + 0.4\theta^2 = 0.304$  (by  $h$ -group);
    - ▶  $p_0 = 0.6p_u + 0.4p_d = 0.6496 > E_0^h \left[ \tilde{\theta} \right] = 0.5776$ .
  - ▶ The key insight of Harrison and Kreps (1978): optimists are willing to pay a price higher than their already optimistic belief because of the resale option.

# Beliefs and Learning

- ▶ Agents' beliefs on date 0 represent their priors. Each agent can update belief on date 1 based on the realized fundamental shock.
- ▶ Suppose agent  $i$ 's prior has beta distribution with  $(\alpha^i, \beta^i)$ .
  - ▶ The mean of this distribution is  $\pi_0^i \equiv \frac{\alpha^i}{\gamma^i}$  where  $\gamma^i \equiv \alpha^i + \beta^i$ .
  - ▶  $\pi_0^i$  is mean,  $\gamma^i$  captures confidence.
- ▶ His posterior on date 1 also has beta distribution with confidence  $\gamma^i + 1$ 
  - ▶ In state  $u$ , the posterior mean is  $\pi_u^i = \frac{\gamma^i}{\gamma^i + 1} \pi_0^i + \frac{1}{\gamma^i + 1}$ .
  - ▶ In state  $d$ , the posterior mean is  $\pi_d^i = \frac{\gamma^i}{\gamma^i + 1} \pi_0^i$ .
- ▶ Even if  $\pi_0^h > \pi_0^l$ , the beliefs can flip on date 1 :
  - ▶  $\pi_u^h$  can be lower than  $\pi_u^l$  if  $\gamma^h$  is sufficiently higher than  $\gamma^l$ .
  - ▶ Then,  $h$ -agent sells his asset to  $l$ -agent for a profit.
- ▶ The flip of beliefs generates trades and motivates ex ante speculative incentives.

# A Recursive Model in Continuous Time

- ▶ How is trading intensity related to price bubble?
- ▶ Scheinkman and Xiong (2003, JPE) provide a recursive model to analyze this question.
- ▶ Consider a single risky asset:

$$dD_t = f_t dt + \sigma_D dZ_t^D$$

whose drift rate is unobservable but follows

$$df_t = -\lambda(f_t - \bar{f})dt + \sigma_f dZ_t^f$$

- ▶ Two sets of risk-neutral agents,  $A$  and  $B$ . They observe  $D_t$  and two public signals generated by:

$$\begin{aligned} ds_t^A &= f_t dt + \sigma_s dZ_t^A \\ ds_t^B &= f_t dt + \sigma_s dZ_t^B \end{aligned}$$

## *A Recursive Model in Continuous Time (cont'd)*

- ▶ Group-A agents are overconfident about their favorite signal  $A$  and believe it is generated by

$$ds_t^A = f_t dt + \sigma_s \phi dZ_t^f + \sigma_s \sqrt{1 - \phi^2} dZ_t^A.$$

Group-B agents are overconfident about their favorite signal  $B$  and believe it is generated by

$$ds_t^B = f_t dt + \sigma_s \phi dZ_t^f + \sigma_s \sqrt{1 - \phi^2} dZ_t^B.$$

## A Recursive Model in Continuous Time (cont'd)

- ▶ In steady state, agent  $i$ 's posterior

$$f_t | \left\{ D_\tau, s_\tau^A, s_\tau^B \right\}_{\tau=0}^t \sim N \left( \hat{f}_t^i, \gamma \right)$$

with

$$\begin{aligned} d\hat{f}_t^A = & -\lambda(\hat{f}_t^A - \bar{f})dt + \frac{\phi\sigma_s\sigma_f + \gamma}{\sigma_s^2}(ds_t^A - \hat{f}_t^A dt) \\ & + \frac{\gamma}{\sigma_s^2}(ds_t^B - \hat{f}_t^A dt) + \frac{\gamma}{\sigma_D^2}(dD_t - \hat{f}_t^A dt) \end{aligned}$$

and

$$\begin{aligned} d\hat{f}_t^B = & -\lambda(\hat{f}_t^B - \bar{f})dt + \frac{\gamma}{\sigma_s^2}(ds_t^A - \hat{f}_t^B dt) \\ & + \frac{\phi\sigma_s\sigma_f + \gamma}{\sigma_s^2}(ds_t^B - \hat{f}_t^B dt) + \frac{\gamma}{\sigma_D^2}(dD_t - \hat{f}_t^B dt) \end{aligned}$$

## A Recursive Model in Continuous Time (cont'd)

- ▶ Let  $g_A$  and  $g_B$  denote the differences in beliefs:

$$g^A = \hat{f}^B - \hat{f}^A, \quad g^B = \hat{f}^A - \hat{f}^B.$$

- ▶ From group-A investors' perspective:

$$dg_t^A = -\rho g_t^A dt + \sigma_g dW_t^{A,g},$$

where

$$\rho = \sqrt{\left(\lambda + \phi \frac{\sigma_f}{\sigma_s}\right)^2 + (1 - \phi^2)\sigma_f^2 \left(\frac{2}{\sigma_s^2} + \frac{1}{\sigma_D^2}\right)},$$
$$\sigma_g = \sqrt{2}\phi\sigma_f,$$

and  $W^{A,g}$  is a standard Wiener process.

- ▶ Similarly, for agents in group  $B$ ,  $g^B$  satisfies:

$$dg_t^B = -\rho g_t^B dt + \sigma_g dW_t^{B,g},$$

where  $W^{B,g}$  is a standard Wiener process.

## A Recursive Model in Continuous Time (cont'd)

- ▶ Assume that both groups A and B are large, no short selling, and risk-free borrowing available at rate  $r$ .
- ▶ Let  $o \in \{A, B\}$  denote the current owner,  $\bar{o}$  the other group. Then,

$$p_t^o = \sup_{\tau \geq 0} E_t^o \left[ \int_t^{t+\tau} e^{-r(s-t)} dD_s + e^{-r\tau} (p_{t+\tau}^{\bar{o}} - c) \right],$$

where  $\tau$  is a stopping time,  $c$  is a transaction cost charged to the seller, and  $p_{t+\tau}^{\bar{o}}$  is the reservation value of the buyer at  $t + \tau$ .

- ▶ A conjecture of the price function

$$p_t^o = p^o(\hat{f}_t^o, g_t^o) = \frac{\bar{f}}{r} + \frac{\hat{f}_t^o - \bar{f}}{r + \lambda} + q(g_t^o),$$

with  $q > 0$  and  $q' > 0$ .

- ▶ The resale option value satisfies

$$q(g_t^o) = \sup_{\tau \geq 0} E_t^o \left[ \left( \frac{g_{t+\tau}^o}{r + \lambda} + q(g_{t+\tau}^{\bar{o}}) - c \right) e^{-r\tau} \right].$$

- ▶ Trading occurs for the first time that  $g^o$  hits a threshold  $k^*$ .

# Effects of Overconfidence

- Higher overconfidence  $\Rightarrow$  more volatile disagreement  $\Rightarrow$  more trading & bigger bubble

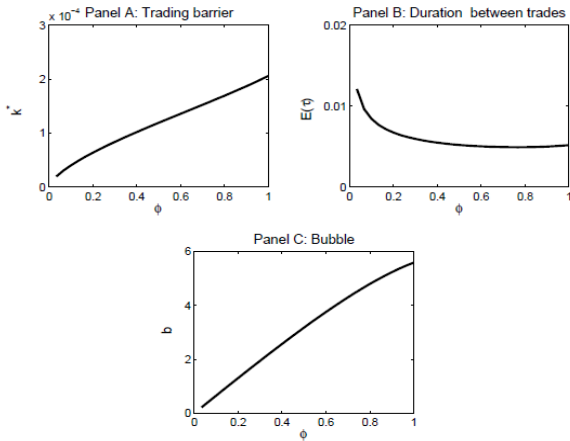


Figure 1: Effect of overconfidence

# Effects of Information

- More information can lead to more disagreement, and thus more trading & bigger bubble.

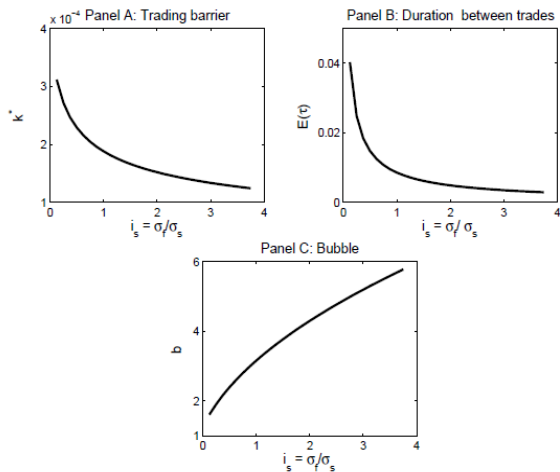


Figure 2: Effect of information

# Effects of Trading Cost

- Tobin's tax can greatly reduce trading, but has only a second-order effect on price bubble.

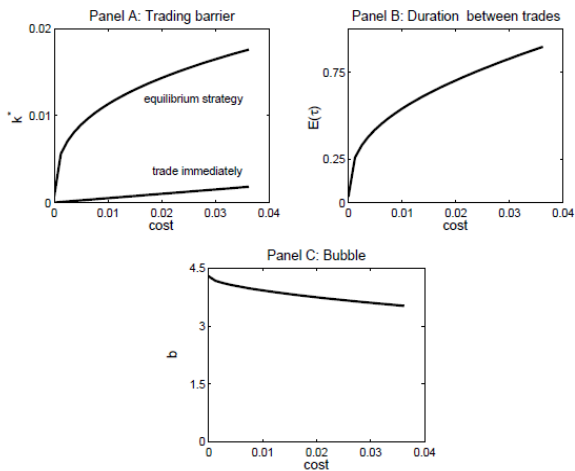


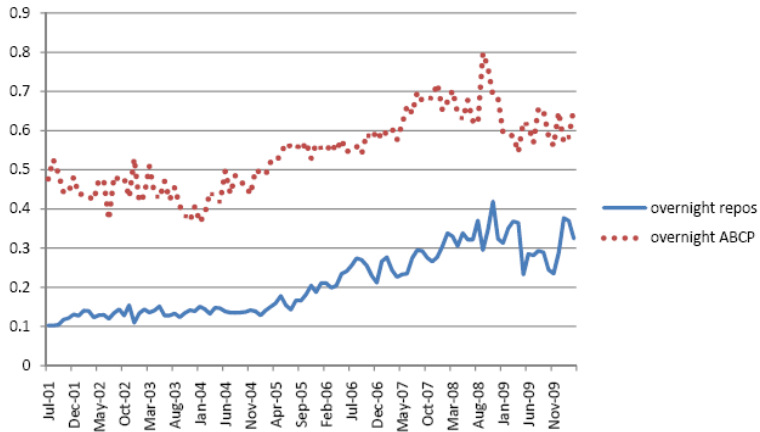
Figure 3: Effect of transaction cost

## Part II: Financing Bubbles and Debt Crises

- ▶ Leverages and debt structure emerged at the center of the recent financial crisis:
  - ▶ Financial institutions used large leverages.
  - ▶ Debt maturity dramatically shortened before 2007.
  - ▶ Failure to roll over short-term debt triggered the crisis and systemic liquidity risk.
- ▶ How do optimists finance their speculation if they don't have enough cash?
  - ▶ Geanakoplos (2009): collateralized debt
- ▶ Focus on a model by He and Xiong (2010) on "Heterogeneous Beliefs and Short-term Credit Booms".
  - ▶ Joint choices of leverage and debt maturity

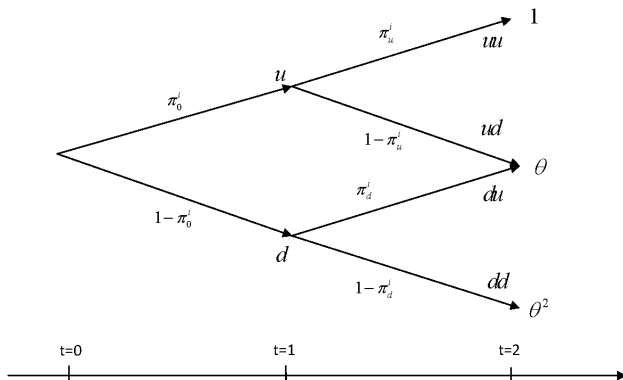
## Maturity Shortening Before the Crisis

- ▶ Fraction of monthly issuance of overnight repos and ABCP



# The Model Setup

- ▶ The long-term risky asset pays off at  $t = 2$  as a binomial tree.
- ▶ Two groups of agents holding heterogeneous beliefs.
  - ▶ We denote optimists by  $h$  and pessimists by  $l$ .
  - ▶ In the basic model, we let  $\pi_n^h > \pi_n^l$  for any  $n \in \{0, u, d\}$ .



# Asset Market

- ▶ 1 unit of risky asset supply,  $\mu \in (0, 1)$  units of optimists.
- ▶ On date 0, each optimist is endowed with 1 unit of asset and  $c$  dollars of cash.
  - ▶ Optimism motivates them to buy the remaining  $1 - \mu$  units of assets from pessimists.
- ▶ The pessimists sit on the sideline, and can provide credit to the optimists.
  - ▶ We assume they always have sufficient cash to provide competitive financing to the optimists.
  - ▶ Their belief affects the financing cost.
- ▶ Risk neutral agents, zero interest rate.
- ▶ Short sales are not allowed.

# Collateralized Debt Financing

- ▶ The optimists use their asset holdings as collateral to obtain debt financing.
- ▶ Only consider standard non-contingent debt contracts.
  - ▶ A non-contingent debt contract specifies a constant debt payment (face value) at maturity unless the borrower defaults.
  - ▶ By shifting control to the creditor after price declination, debt disciplines excessive risk-taking by optimists.
- ▶ In equilibrium, optimists always choose face value in  $[\theta^2, \theta]$ , as long as the asset price is between the optimists' and pessimists' asset valuation.
- ▶ In equilibrium, optimists do not save cash.
  - ▶ It is not desirable for any optimist to sell his asset on date 1.
  - ▶ He has to refinance his debt on date 1 if he uses short-term debt, or loses his asset to the creditor.

## Long-Term Debt

- ▶ A long-term debt contract, collateralized by one unit of the asset.
  - ▶ It matures on date 2 with a face value of  $F_L \in [\theta^2, \theta]$ .
  - ▶ The random debt payment  $\tilde{D}_L(F_L) = \min(F_L, \tilde{\theta})$ .

- ▶ On date 0, pessimistic creditors provide credit:

$$C_L(F_L) = E_0^l[\tilde{D}_L] = \left(1 - (1 - \pi_0^l)(1 - \pi_d^l)\right) F_L + (1 - \pi_0^l)(1 - \pi_d^l) \theta^2.$$

- ▶ Financing cost to the optimistic borrower:

$$E_0^h[\tilde{D}_L] = \left(1 - (1 - \pi_0^h)(1 - \pi_d^h)\right) F_L + (1 - \pi_0^h)(1 - \pi_d^h) \theta^2.$$

- ▶ Risky debt ( $F_L > \theta^2$ ) is costly because the creditor undervalues the payment in the higher states.
  - ▶ The risk-free debt ( $F_L = \theta^2$ ) is fairly valued but limits leverage.
  - ▶ What if the borrower wants a larger leverage?

## Short-Term Debt

- ▶ ST debt matures on date 1, with face value  $F_S \in [\theta^2, \theta]$ .
- ▶ The borrower refinances at  $t = 1$  by promising a new debt payment  $F_{S,1}$  at  $t = 2$ :  $E_n^l [\min(F_{S,1}, \tilde{\theta})] = F_S$ .
  - ▶ In state  $u$ , the borrower just needs to promise  $F_{S,1} = F_S$ .
  - ▶ In state  $d$ , the maximum credit he can raise is

$$K_d \equiv \mathbb{E}_d^l [\min(\theta, \tilde{\theta})] = \pi_d^l \theta + (1 - \pi_d^l) \theta^2 < \theta.$$

1.  $F_S \in [\theta^2, K_d]$ . Riskless with date-0 credit  $C_S(F_S) = F_S$ .
  - ▶ Risk-free ST debt can raise as much as  $K_d$ , higher than  $\theta^2$ .
  - ▶ In state  $d$ , refinance requires new risky debt with  $F_{S,1} \geq F_S \geq \theta^2$ .
2.  $F_S \in (K_d, \theta]$ . Risky.
  - ▶ in state  $d$ , the borrower forfeits the asset to the creditor.

## Position of Optimists

- ▶ Suppose that an optimist uses a contract  $\tilde{D}$  and obtains an initial credit of  $C(\tilde{D}) \equiv \mathbb{E}_0^l[\tilde{D}]$ .
- ▶ Besides 1 unit of asset endowment, he buys additional  $x$  units from the market.
  - ▶ Collateralized borrowing. He can borrow  $(1+x)C(\tilde{D})$  in total.
- ▶ Budget constraint:  $c + (1+x)C(\tilde{D}) = xp_0 \Rightarrow x = \frac{c+C(\tilde{D})}{p_0-C(\tilde{D})}$ .
  - ▶ Assuming he does not hold any cash, which is verified in equilibrium.
- ▶ His date-0 utility is

$$V(\tilde{D}) = \underbrace{\frac{c+p_0}{p_0-C(\tilde{D})}}_{\text{leverage effect}} \underbrace{\left[ \mathbb{E}_0^h(\tilde{\theta}) - \mathbb{E}_0^h(\tilde{D}) \right]}_{\text{debt-cost effect}}$$

## Maturity Choice

- ▶ Consider two ST and LT contracts giving the same date-0 credit (i.e., fixing the leverage effect).
- ▶ Debt-cost effect: ST debt has lower cost if and only if

$$\frac{\pi_0^h}{\pi_0^l} > \frac{(1 - \pi_0^h) \pi_d^h}{(1 - \pi_0^l) \pi_d^l}.$$

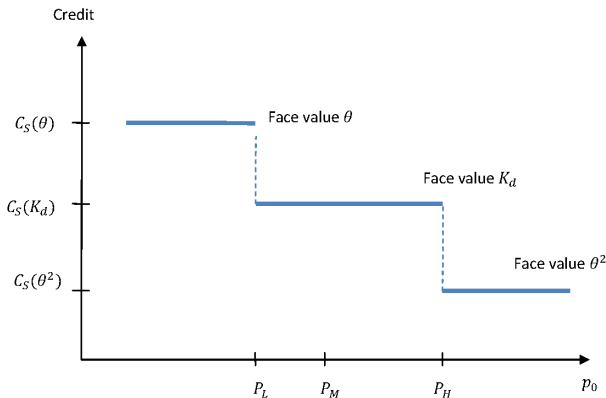
- ▶ ST debt needs refinancing: better or same term after good news, but worse term after bad news.
  - ▶ Pay less in high states, more in low states. preferred by optimists!
  - ▶ Initial belief dispersion at  $t = 0$  stimulates speculative incentives.
- ▶ After bad news (state  $d$ ), belief dispersion leads to rollover risk.
  - ▶ The refinancing  $F_{S,1}$  payment is undervalued by the creditor.
  - ▶ Rollover risk is endogenously determined by heterogeneous beliefs.

## Maturity Choice: The Static Intuition

- ▶ Geanakoplos (2009): optimists always prefer the maximum risk-free short-term leverage.
- ▶ Examine the short-term  $K_d$  contract: initially risk-free.
  - ▶ In state  $u$ , refinance by another risk-free contract;
  - ▶ In state  $d$ , refinance by turning the asset to creditor.
- ▶ This intuition ignores the rollover risk and does not hold if the future belief dispersion in state  $d$  is sufficiently large.
- ▶ Our model shows that short-term debt is desirable only if initial belief dispersion is high and future dispersion in state  $d$  is low.
  - ▶ Long-term debt could be optimal because it hedges the financing cost against future downturns.

## Optimal Short-term Debt Face Value: Leverage Choice

- ▶ Suppose that short-term debt is desirable.
  - ▶ The default risk is different for  $F_S$  inside  $[\theta^2, K_d]$  and  $[K_d, \theta]$ .
- ▶ Two thresholds  $P_H$  and  $P_L$  for price  $p_0$ . The higher the asset price  $p_0$ , the lower the leverage that the optimists will take.



## Equilibrium of Asset and Credit Markets on Date 0

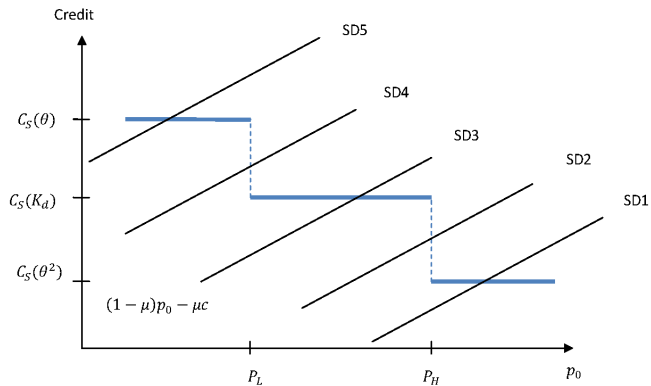
- ▶ Recall the optimists (with measure  $\mu$ ) buy  $x = \frac{c + C(\tilde{D})}{p_0 - C(\tilde{D})}$  units from the market, and pessimists sell  $1 - \mu$  to the market.
- ▶ Market clearing: the optimists' asset purchases  $\mu x = 1 - \mu$ .
- ▶ If all the buyers use the same debt contract  $\tilde{D}(p_0)$ , then

$$\mu \frac{c + C(\tilde{D}(p_0))}{p_0 - C(\tilde{D}(p_0))} = 1 - \mu$$

which is equivalent to

$$\underbrace{C(\tilde{D}(p_0))}_{\text{credit demand}} = \underbrace{(1 - \mu)p_0 - \mu c}_{\text{cash shortfall}}$$

# Market Equilibrium



# Equilibrium on Date 1

- ▶ We look for shadow price on date 1, which has two states  $u$  and  $d$ .
- ▶ In state  $u$ , the optimistic asset holders are in a good financial situation, and the asset price is determined by their valuation:

$$p_u = \mathbb{E}_u^h [\tilde{\theta}] = \pi_u^h + (1 - \pi_u^h) \theta.$$

- ▶ In state  $d$ , the equilibrium depends on the date-0 debt contracts:
  - ▶ If all asset holders use riskless debt contracts, then optimists who hold the asset determines the price:

$$p_d = \mathbb{E}_d^h [\tilde{\theta}] = \pi_d^h \theta + (1 - \pi_d^h) \theta^2.$$

- ▶ Otherwise, some asset holders are forced to transfer assets to pessimistic creditors:

$$p_d = \mathbb{E}_d^l [\tilde{\theta}] = \pi_d^l \theta + (1 - \pi_d^l) \theta^2.$$

# Heterogeneous Beliefs and Asset Price Cycles

- ▶ Standard Miller result: in the absence of short-sales, heterogeneous beliefs cause asset overvaluation.
- ▶ We evaluate this result after accounting for optimists' financing cost.
- ▶ We use the following baseline parameters:

$$\begin{aligned}\mu &= 0.3, c = 0.5, \theta = 0.4, \pi_0^h = 0.7, \pi_0^l = 0.3, \\ \pi_u^h &= 0.6, \pi_u^l = 0.4, \pi_d^h = 0.6, \pi_d^l = 0.4.\end{aligned}$$

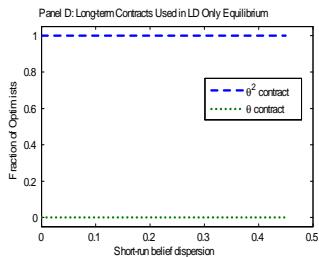
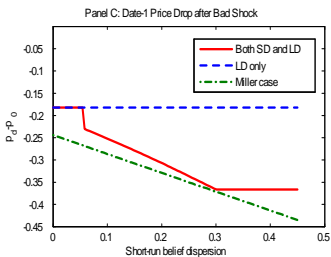
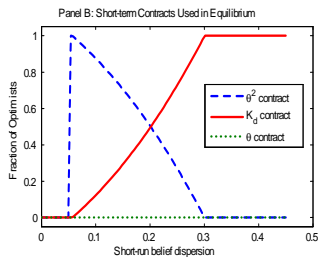
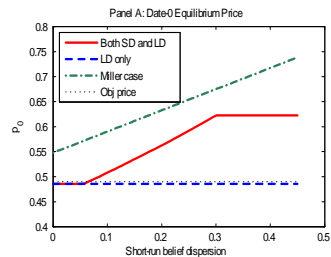
- ▶ To evaluate the effect of initial belief dispersion on date 0 (speculative incentives), we let

$$\pi_0^h = 0.5 + \delta_0 \text{ and } \pi_0^l = 0.5 - \delta_0.$$

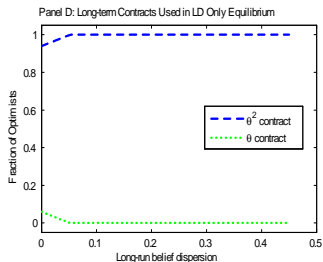
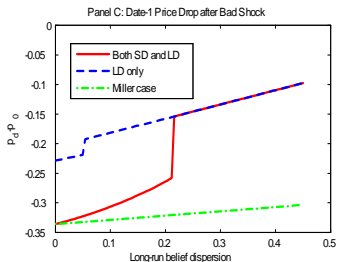
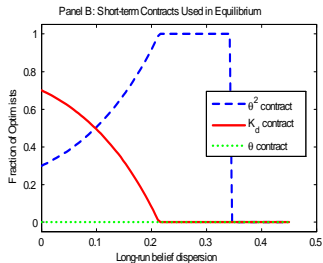
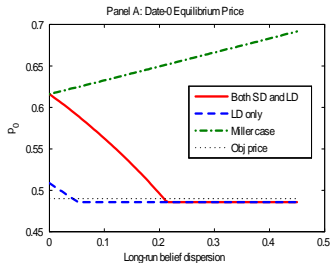
- ▶ To evaluate the effect of belief dispersion in state  $d$  of date 1 (rollover risk), we let

$$\pi_d^h = 0.5 + \delta_d, \text{ and } \pi_d^l = 0.5 - \delta_d.$$

# The Initial Belief Dispersion on Date 0



# The Future Belief Dispersion in State $d$ of Date 1



## *Discussion on Short-term Credit Booms*

- ▶ Several episodes of short-term credit booms:
  - ▶ before the credit crisis of 2007-2008;
  - ▶ before the debt crises of emerging economies in 1990s;
  - ▶ before the great crash of 1929.
- ▶ A short-term credit boom can fuel an asset-market boom and then exacerbate the downturn after the asset fundamental deteriorates.
  - ▶ The importance of financing choices for understanding asset-market dynamics and financial crises.
- ▶ This model characterizes a set of conditions for short-term credit booms to emerge:
  - ▶ large short-term belief dispersion;
  - ▶ and future belief convergence.

# *Discussion on Heterogeneous Beliefs and Asset Bubbles*

- ▶ There is a large literature on asset bubbles generated by heterogeneous beliefs and short-sales constraints.
  - ▶ Miller (1977) and Chen, Hong and Stein (2002): a larger belief dispersion leads to a higher asset price and a lower expected return.
  - ▶ Harrison and Kreps (1978), Morris (1996) and Scheinkman and Xiong (2003): more volatile belief dispersion leads to more valuable resale option and more frequent asset trading.
- ▶ These studies ignore financing cost and heterogeneous beliefs in different horizons.
- ▶ This model highlights the differences between initial and future belief dispersion when optimists need financing.
  - ▶ A higher initial belief dispersion can lead to a higher asset price;
  - ▶ while a higher future belief dispersion after fundamental deterioration reduces asset price.

## Related Literature

- ▶ Credit contraction during crises.
  - ▶ Procyclical leverages: Adrian and Shin (2008) and Geanakoplos (2009);
  - ▶ Increased margins in crises, e.g., Brunnermeier and Pedersen (2009);
  - ▶ Shortened debt maturity during crises, e.g., He and Xiong (2009a) and Brunnermeier and Oehmke (2009).
- ▶ Reasons for pervasive use of ST debt:
  - ▶ Agency problems inside firms: Calomiris and Kahn (1991), Diamond and Rajan (2009).
  - ▶ ST debt is less information sensitive: Gorton and Pennacchi (1990).
  - ▶ Signaling: Diamond (1991).
  - ▶ This model emphasizes speculative incentives as a driving force, and links debt maturity choice to asset market dynamics.
- ▶ Heterogeneous beliefs and security designs:
  - ▶ Garmaise (2001), and Landier and Thesmar (2008).